

Radical Expressions Multiplication

Multiplying Radical Expressions is the same as multiplying polynomials. You will use Exponent Rules & FOIL.

Examples:

$$\sqrt[3]{4} * \sqrt[3]{4} \xrightarrow{\text{one_way}} \sqrt[3]{4 * 4} \rightarrow \sqrt[3]{2^4} \rightarrow \sqrt[3]{2^{3+1}} \rightarrow \sqrt[3]{2^3 2^1} \rightarrow 2\sqrt[3]{2^1} \rightarrow 2\sqrt[3]{2}$$

$$\sqrt{x} * \sqrt[4]{16y^2} \xrightarrow{\text{one_way}} x^{\frac{1}{2}} (2^4 y^2)^{\frac{1}{4}} \xrightarrow{\text{note_2_can_be_removed}} 2x^{\frac{1}{2}} (y^2)^{\frac{1}{4}} \xrightarrow{\text{rewrite } \frac{1}{2} \text{ as } \frac{2}{4}} 2x^{\frac{2}{4}} (y^2)^{\frac{1}{4}} \rightarrow 2(x^2)^{\frac{1}{4}} (y^2)^{\frac{1}{4}} \rightarrow 2(x^2 y^2)^{\frac{1}{4}} \rightarrow 2\sqrt[4]{x^2 y^2}$$

$$(\sqrt{x} + 1)(\sqrt{2} - 3) \xrightarrow{\text{FOIL}} \sqrt{x} * \sqrt{2} - 3\sqrt{x} + 1\sqrt{2} - 3 \rightarrow \sqrt{2x} - 3\sqrt{x} + 1\sqrt{2} - 3$$

$$(\sqrt[3]{x} - 2)(\sqrt[3]{x} + 2) \xrightarrow{\text{FOIL}} \sqrt[3]{x} * \sqrt[3]{x} + 2\sqrt[3]{x} - 2\sqrt[3]{x} - 4 \rightarrow \sqrt[3]{x * x} - 4 \rightarrow \sqrt[3]{x^2} - 4$$

A Radical Expression is Simplified When:

- 1.) The radicand contains no factor greater than 1 that is a perfect power of the index.
- 2.) There is no fraction under the radical.
- 3.) There is no radical in the denominator of an expression.
- 4.) Any exponents under the radical & the index of the radical are relatively prime (no factors in common except 1)